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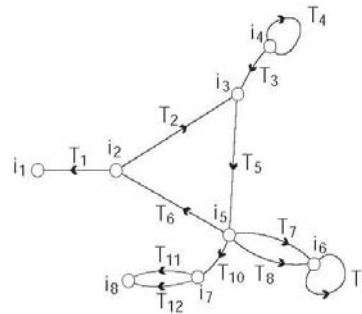
### A Graph of Matrices

Free probability is a variation of probability theory for matrix valued random variables. It has many aspects: combinatorial, analytic, theoretical, and applied. I will discuss a problem on a graph of matrices arising from a random matrix problem in free probability.

Let  $G = (E, V)$  be a graph and  $T$  a map from  $E$  to the  $N \times N$  matrices. We write the matrix elements of  $T(e)$  as  $\{t_{ij}^{(e)}\}$  and let

$$S_G(T) = \sum_{i: V \rightarrow [N]} \prod_{e \in E} t_{i_s(e) i_t(e)}^{(e)}$$

where  $i$  runs over all functions from  $V$  to  $[N] = \{1, 2, 3, \dots, N\}$ . For example if the the graph  $G$  is



the corresponding sum is

$$S_G(T) = \sum_{i_1, i_2, \dots, i_7=1}^N t_{i_1 i_2}^{(1)} t_{i_2 i_3}^{(2)} t_{i_3 i_4}^{(3)} t_{i_4 i_5}^{(4)} t_{i_5 i_6}^{(5)} t_{i_6 i_7}^{(6)} t_{i_7 i_8}^{(7)} t_{i_8 i_1}^{(8)} t_{i_1 i_2}^{(9)} t_{i_2 i_3}^{(10)} t_{i_3 i_4}^{(11)} t_{i_4 i_5}^{(12)}$$

The question we wish to address is the dependence of  $S_G(T)$  on  $N$ , which as we shall show has a surprisingly simple answer.