

# GRADUATE SEMINAR

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## Pure Matrix States on Operator System Tensor Products

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**3:30 p.m.**

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**Abstract:** A theorem of Namioka and Phelps states that for order unit spaces,  $E_1$  and  $E_2$ , and an order unit tensor product  $\otimes_\sigma$ , the scalar state space  $\mathcal{S}_1(E_1)$  is simplex-like if and only if any  $s \in \mathcal{S}_1(E_1 \otimes_\sigma E_2)$  can be expressed as  $s = s_1 \cdot s_2$  for  $s_1 \in \mathcal{S}_1(E_1)$  and  $s_2 \in \mathcal{S}_1(E_2)$ . This result can be used to show that for any order unit tensor products  $\otimes_\sigma, \otimes_\tau$  that  $\mathcal{S}_1(E_1 \otimes_\sigma E_2) = \mathcal{S}_1(E_1 \otimes_\tau E_2)$  if and only if  $\mathcal{S}_1(E_1)$  is simplex-like. My talk will demonstrate a partial analogue of these theorems in the case where  $E_1$  and  $E_2$  are operator systems and when the scalar state spaces are replaced with matrix state spaces.